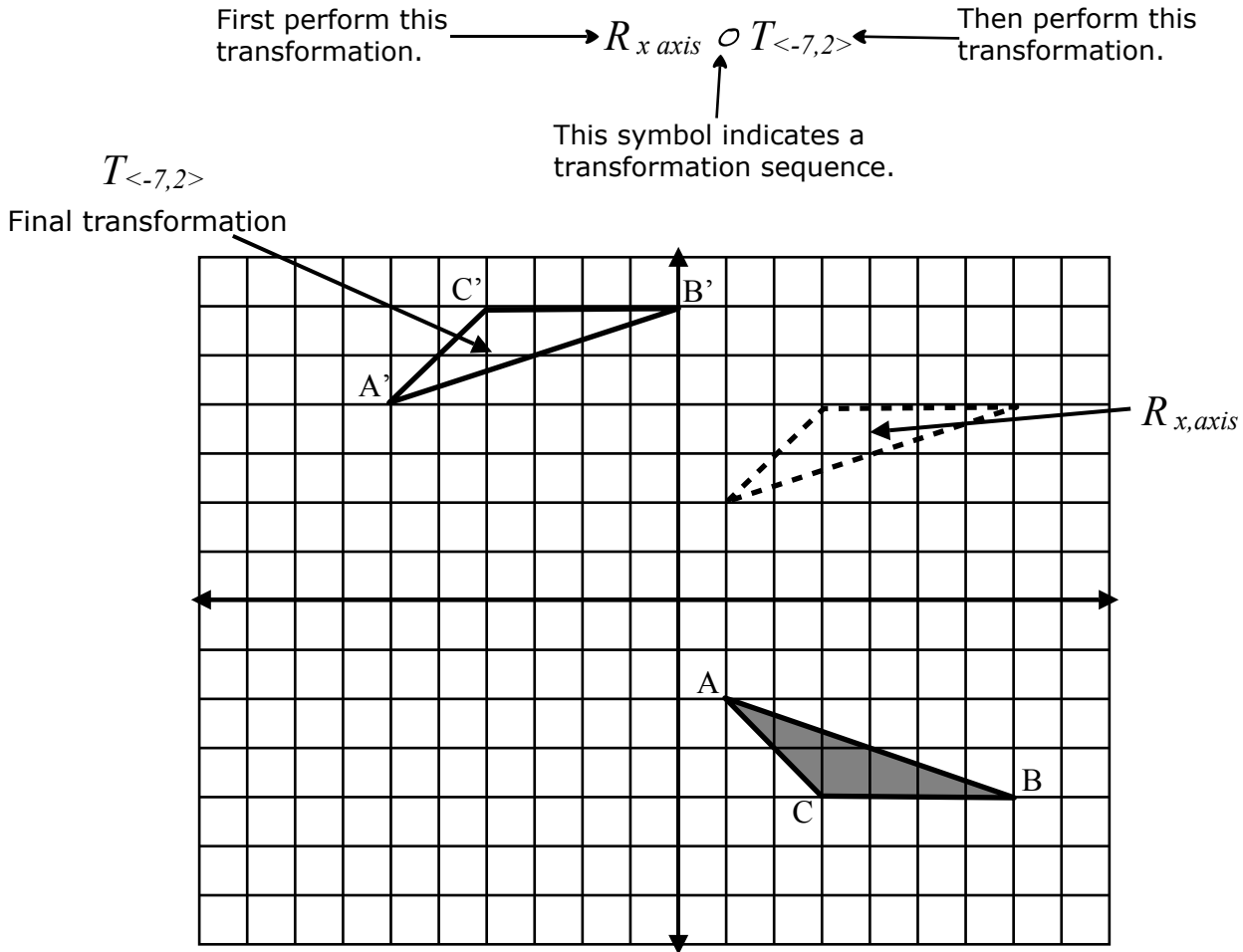


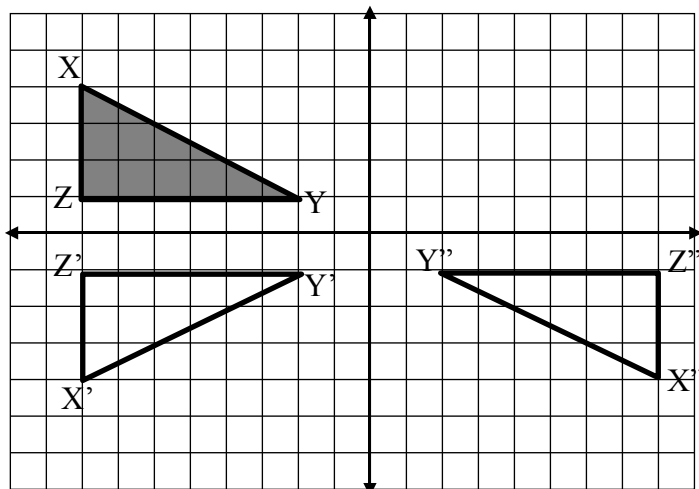
## Transformation Sequences

**Transformation Sequence:** A transformation sequence is 2 or more transformations performed one after the other on the same pre-image. Here is an example.



Sometimes you might be asked to plot each stage of the transformation. That would look like this.

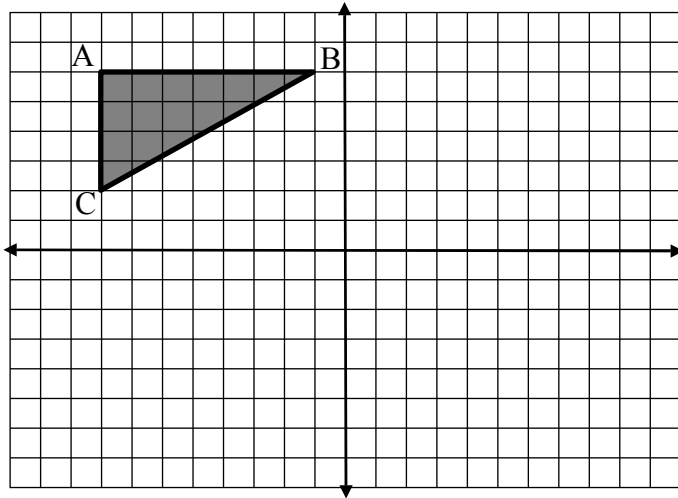
**Plot each stage of the transformation  $R_{x, axis} \circ R_{y, axis}$ .**



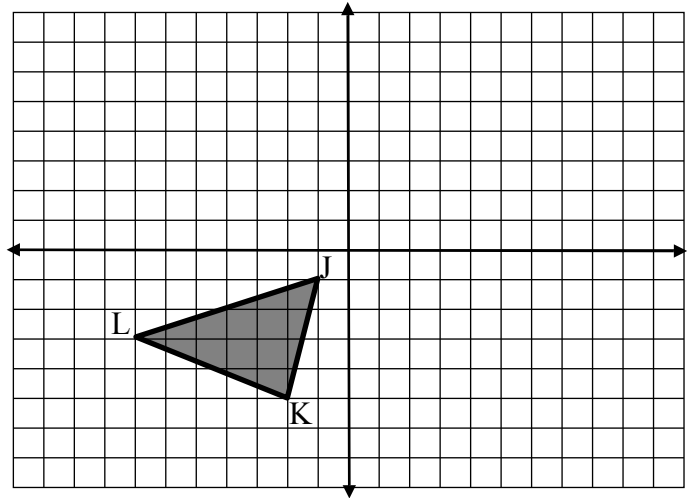
In the example to the left notice that the first transformation has the labels  $X'$ ,  $Y'$ , and  $Z'$  (“x prime,” “y prime,” and “z prime”). The second one has the labels  $X''$ ,  $Y''$ , and  $Z''$ . We say “x double-prime,” “y double-prime,” and “z double-prime.”

**Directions:** Perform the following transformation sequences. Plot each stage of the sequence. Use patty paper, geometry software, or any other method.

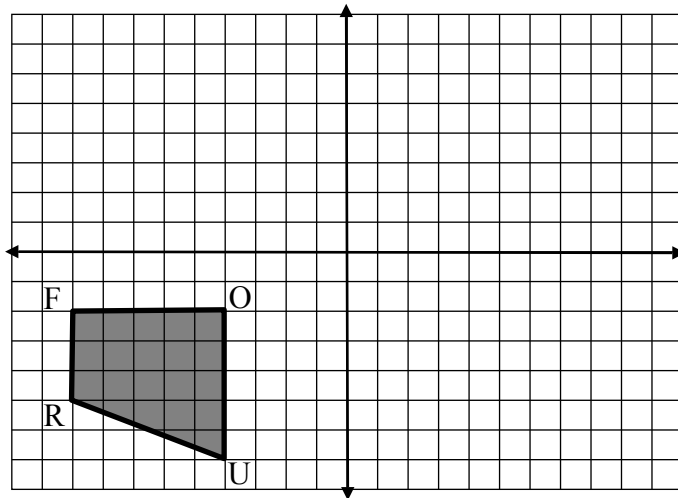
1.  $R_{y \text{ axis}} \circ R_{x \text{ axis}}$



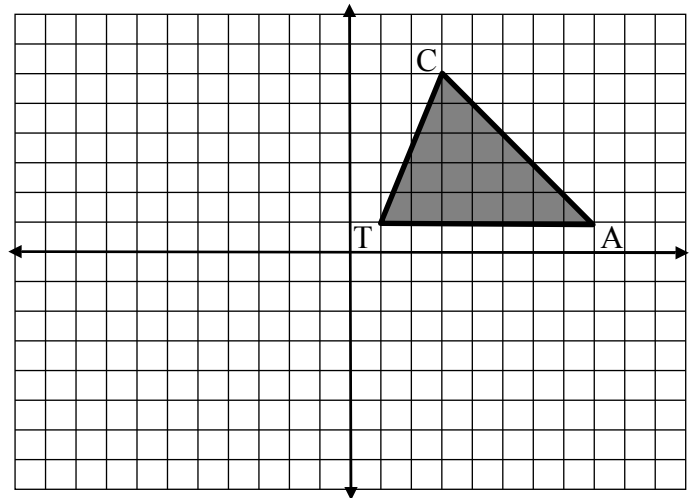
2.  $R_O, 90^\circ \circ R_{x \text{ axis}}$



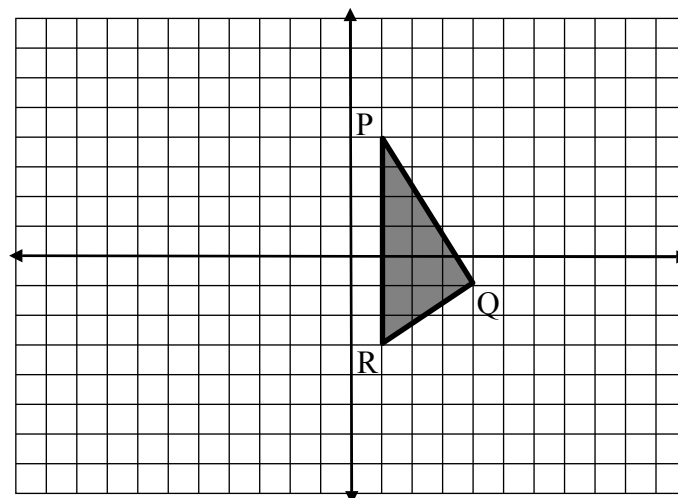
3.  $T_{\langle 2, 6 \rangle} \circ R_O, 180^\circ$



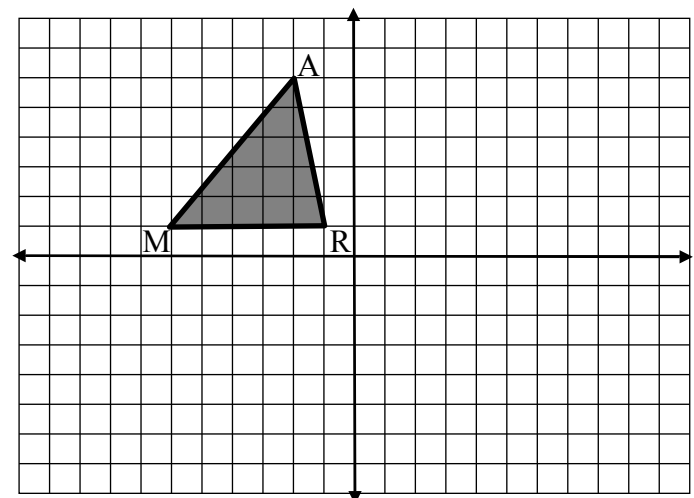
4.  $R_O, 90^\circ \circ R_O, 90^\circ$



4.  $R_{y \text{ axis}} \circ R_{x=-5}$



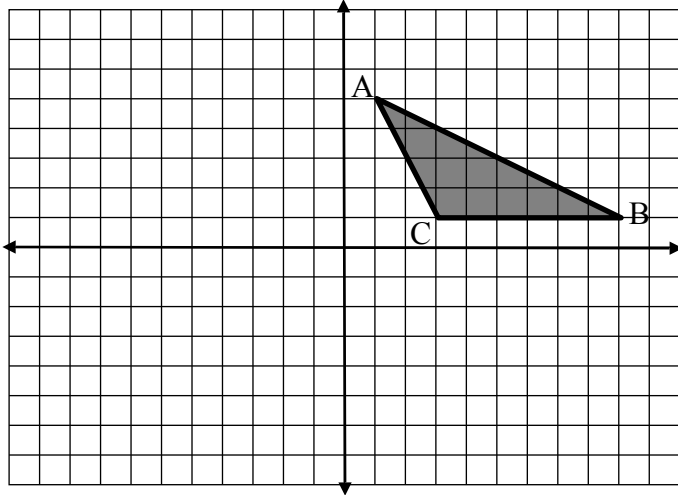
4.  $R_{x \text{ axis}} \circ R_O, 90^\circ$



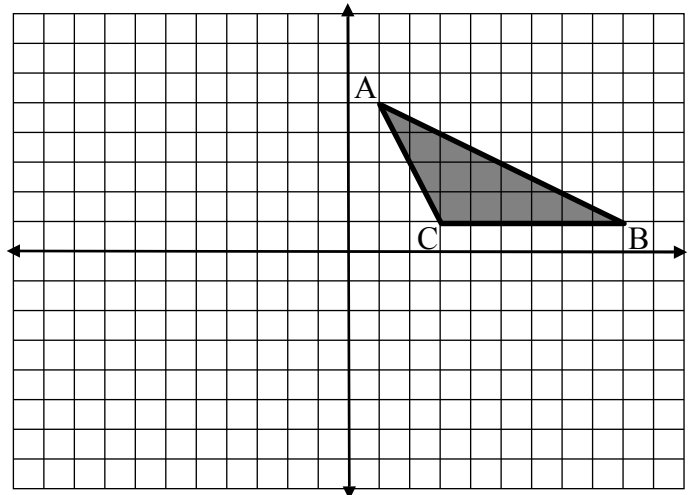
**Directions:** Perform the following transformation sequences. Plot each stage of the sequence. Use patty paper, geometry software, or any other method, and answer the questions .

**1.** What do you think? Does the order in which you perform a transformation sequence effect the final image? Explain your reasoning.

**2a.**  $R_{O, 180^\circ} \circ R_{x \text{ axis}}$

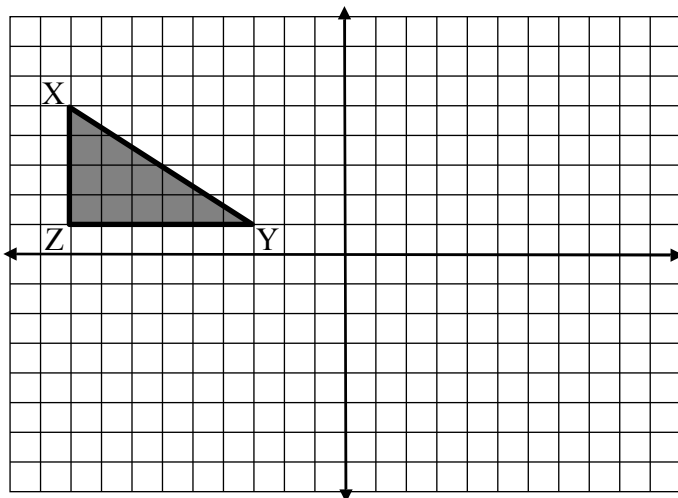


**2b.**  $R_{x \text{ axis}} \circ R_{O, 180^\circ}$

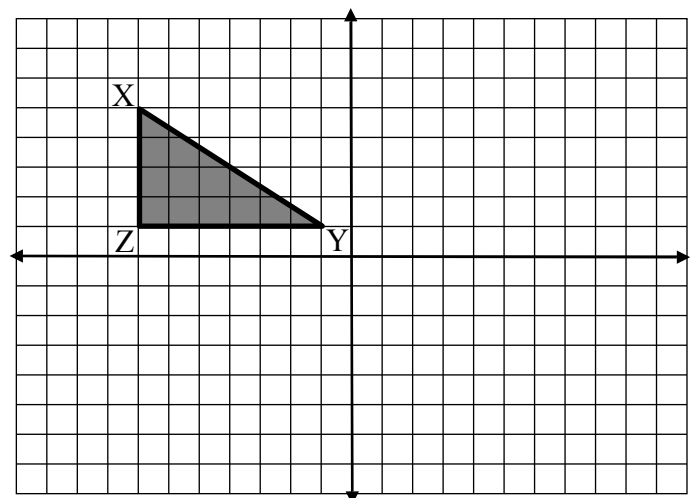


**2c.** Did performing the same transformation sequence in the reverse order change the position of the final image? Why?

**3a.**  $T_{\langle 8, 1 \rangle} \circ R_{x \text{ axis}}$



**3a.**  $R_{x \text{ axis}} \circ T_{\langle 8, 1 \rangle}$

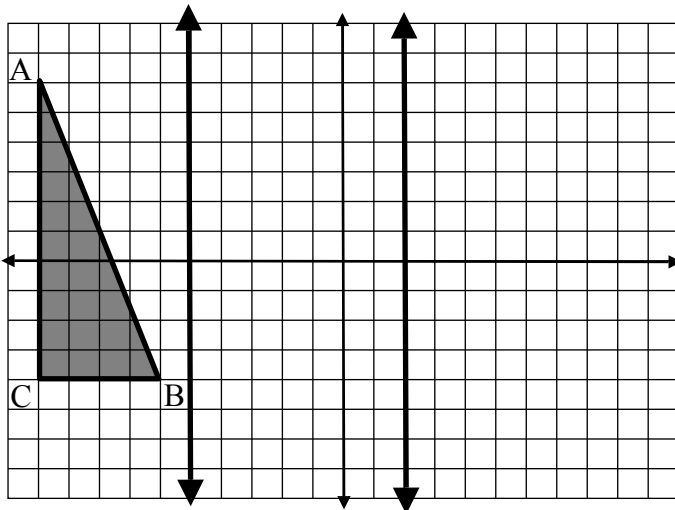


**2c.** Did performing the transformation in the reverse order change the position of the final image? Why?

**Directions:** Perform the following transformation sequences. Plot each stage of the sequence. Use patty paper, geometry software, or any other method, and answer the questions .

1. What do you think will happen if you reflect a figure twice over two parallel lines?

2a.  $R_{x=-5} \circ R_{x=2}$

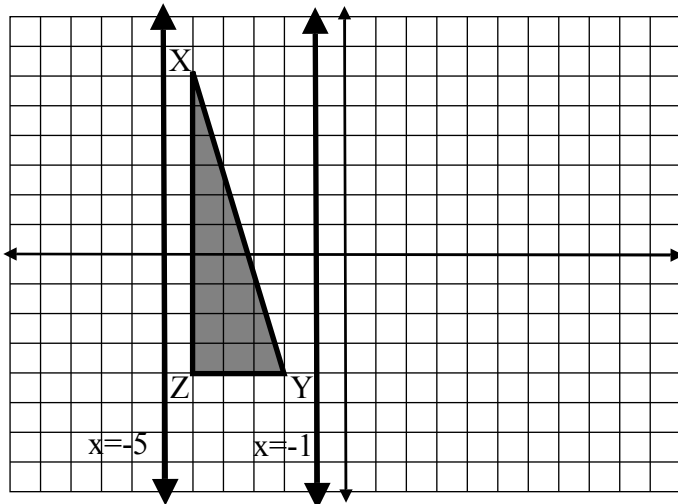


2b. What kind of transformation is the result from ABC to A''B''C'' ?

2c. Describe the transformation. What is the distance between A and A''?

2d. What is the relationship between the distance of the transformation and the distance between the parallel lines?

3a.  $R_{x=-5} \circ R_{x=-1}$



3b. What kind of transformation is the result from XYZ to X''Y''Z'' ?

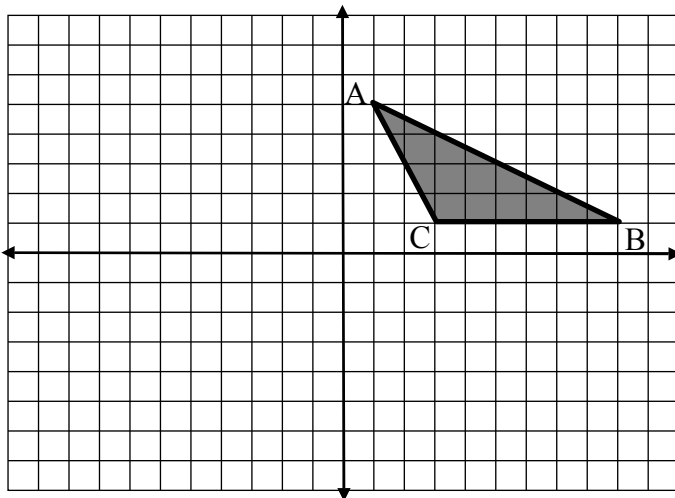
3c. Describe the transformation. What is the distance between X and X''?

3d. What is the relationship between the distance of the transformation and the distance between the parallel lines?

**Directions:** Perform the following transformation sequences. Plot each stage of the sequence. Use patty paper, geometry software, or any other method, and answer the questions .

1. What do think will happen if you reflect a figure twice over two intersecting lines?

2a.  $R_{x \text{ axis}} \circ R_{y \text{ axis}}$

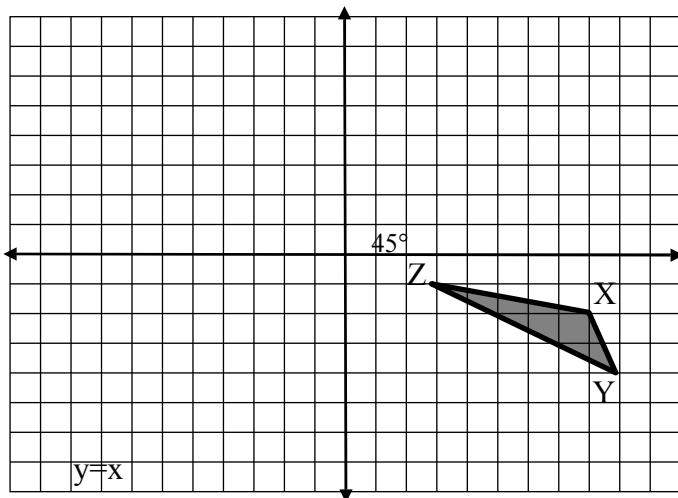


2b. What kind of transformation is the result from ABC to A''B''C'' ?

2c. How did you know what kind of transformation it was?

2d. What is the relationship between the angle that the two axis intersect and the transformation?

3a.  $R_{x \text{ axis}} \circ R_{y=x}$



3b. What kind of transformation is the result from XYZ to X''Y''Z'' ?

3c. How did you know what kind of transformation it was?

3d. What is the relationship between the angle that the two axis intersect and the transformation?